\begin{tabular}{|c|c|c|}
\hline Stage Name \& Examples \& Recording Method \\
\hline Practical Examples \& Doubling using the language of multiplication \& \\
\hline Pictorial Representation \& How many groups of (lots of) 2 are there? \& \begin{tabular}{l}
Mostly pictorial representation: \\
How many groups of two are there? \\
Use of concrete apparatus for the children to physically count and see. Extend to written digit representation.
\end{tabular} \\
\hline Repeated Addition (Number line) \& I have 3 pairs of shoes - how many shoes do I have altogether? \&  \\
\hline Decoding arrays and repeated addition (larger numbers) \& \begin{tabular}{l}
Multiply 5 by 8 \\
How many fives in 35 ? \\
A baker puts 6 buns in 4 rows. How many altogether? \\
Double 32 \\
What is the product of 25 and 4 ?
\end{tabular} \& \begin{tabular}{l}
Describe arrays:
\(\square\)
\(\square\) \(\square\)

$4 \times 3=12$

$$
3 \times 4=12
$$ \\

Plus repeated addition (number lines)
\end{tabular} \\

\hline Grid Method \& | Multiply 31 by 8 |
| :--- |
| Calculate $345 \times 9$ | \& | $23 \times 8=$ |
| :--- |
| 8 $160+24=184$ |
| $72 \times 38=$ $\begin{array}{r} 2100 \\ 560 \\ 60 \\ +\quad 16 \\ \hline 2736 \\ \hline \end{array}$ | \\


\hline Expanded Vertical \& | What is the product of $125 \times 4$ ? |
| :--- |
| Calculate $4346 \times 9$ | \& $\begin{array}{r}4346 \\ \times \quad 9 \\ \hline 54 \\ 360 \\ 2700 \\ 36000 \\ \hline 39114\end{array}$ \\

\hline
\end{tabular}

| Short Multiplication | As above. | $2741 \times 6$ becomes <br> Answer: 16446 |
| :---: | :---: | :---: |
| Long Multiplication | $158 \times 67=10586$ | $\begin{array}{r} 158 \\ \times 67 \\ \hline 1106 \\ 9480 \\ \hline \overline{10586}=\text { Answer } \end{array}$ <br> Find the answer by adding the two calculations together. |
| Multiplying a fraction by a fraction | $3 / 4 \times 2 / 3=$ | $\begin{aligned} & 3 \times 2=6=1 \\ & \frac{4 \times 3}{12} \quad \end{aligned}$ |
| Multiplying a fraction by a whole number | $\frac{2}{3} \times 12=$ | $\begin{gathered} 12=\frac{12}{1} \\ \frac{2}{3} \times \frac{12}{1}=\frac{2 \times 12}{3 \times 1}=\frac{24}{3}=\frac{8}{1}=8 \end{gathered}$ |

